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## META-HEURISTIC ALGORITHMS FOR K-MEANS CLUSTERING: A REVIEW

Alan Fuad Jahwar  
Akre Technical College,  
Duhok Polytechnic University,  
Duhok, Kurdistan Region, Iraq  
alan.jahwar@dpu.edu.krd

Adnan Mohsin Abdulazeez  
Duhok Polytechnic University  
Duhok, Kurdistan Region, Iraq  
adnan.mohsin@dpu.edu.krd

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### ABSTRACT

The increase in the data available attracted the concern of clustering approaches to integrate them coherently and to identify patterns for big data. Hence, Meta-Heuristic algorithms can be better than standard optimization algorithms in some instances. Previously, optimization issues have been considered as significant weaknesses in the K-means algorithm is one of the simplest methods for clustering. and with less additional information it can easily solve the optimization problem. In this paper, a review of clustering k-means algorithm and meta-heuristics algorithms are reviewed.

*Keyword: Machine Learning, Clustering, K-Means, Meta-Heuristic algorithms.*

### 1 INTRODUCTION

The concepts of Machine Learning (ML) come from the domains of computer science and Artificial intelligence (AI), ML deals with systems that can learn from data instead of only executing the programmed commands overtly [1,2,3]. Furthermore, ML is closely linked to optimization and statistics, which brought their theories and approaches to the field. ML is utilized in different computing missions where constructing and programming rule-based, overt algorithms is not feasible. In certain cases, ML, pattern recognition, and data mining share their background [4,5,6].

Samuel (1959) defined ML as the domain that offered computers the capability of learning without being obviously programmed [7,8]. Broadly speaking, the boundary between ML and data mining is sometimes blurs because both adopt similar approaches, and they are considerably interrelated. However, their difference is that ML is dedicated to prediction centered on

known properties which can be taught from training data [9]. Meanwhile, data mining is devoted to the discovery of the (previously) unknown features in the data. These two areas share many characteristics: data mining uses plentiful ML approaches with a various goal in mind. On the other hand, ML uses data mining approaches as unsupervised or supervised learning or as a stage that comes before the enhancement of learning accuracy. The current study: however, is ML centered.

Concerning its functions, there are three kinds of ML, which are the supervised, Semi-supervised and Unsupervised learning. In supervised learning, the teacher provides example inputs and desired outputs, in order to learn a universal rule for mapping inputs to outputs. In supervised learning, the ML task is inferring from tagged training data [10]. Classification is among the instances of the supervised learning that uses labeled data to solve certain problems. In the supervised learning, the ML seeks to trace functions in the labeled training data [11,12,13].

It consists of a group of training examples and every example represents a pair that is made up of an input (usually a vector), and an anticipated output value (supervisory signal). Algorithms that harness Supervised learning analyses training data and creates a deduced function capable of mapping new cases. The ideal setting is expected to help an algorithm select properly the class labeling for unsupervised examples. For this objective, the learning algorithm has to perform generalization from training data to unsupervised cases “reasonably”[14]. The functioning of unsupervised learning algorithms is determined by unlabeled instances, i.e., input where the desired output is unknown. In such a case, the aim is the discovery of the data structure, for instance by means of a cluster analysis, starting from inputs to outputs to generalize a map [15].

K-means has a high clustering speed and performs well in large data sets, but it has poor clustering accuracy, is vulnerable to noise and isolated data, and the value of K needs to be calculated in advance. In order to address the weaknesses of the K-means algorithm, scientists proposed changes in various angles [16,17]. Intelligent algorithms with high global optimization abilities are commonly used in modern industries [18]. Since there are a need for efficient and robust computational algorithms that can solve optimization problems in different fields; this is the practical utility of optimization. [19,20]. Finding a best solution to a problem is optimization. An optimization problem is defined as minimizing or maximizing some function. The optimization problems focus on three factors: (1) a target objective function to minimize or maximize. (2) A set of variables influencing the objective function. (3) A set of constraints that make some unknowns equivalent but exclude others [21].

In many optimization problems there are more than one local optimum solutions. Therefore, it is crucial to choose an appropriate an optimization

method that will not look in the neighborhood of the best solution, misleading the search process. Causing it to get stuck in local minima. Besides, it should also have a mechanism to balance between local and global search. Optimization problems of both the mathematical and combinatorial types are solved using several methods. If the optimization problem is difficult to solve or the search space is big, then classical mathematics would be incapable of finding an optimal solution [22,23].

## **2 Meta-Heuristic Algorithms**

A Meta-heuristic is a continuous iteration of different concepts and structures to find near-optimal solutions. Meta-heuristic algorithms are among these approaches to improve complex problems [24,25]. Meta-heuristic algorithms usually find the global optimum more quickly than ordinary stochastic algorithms. The algorithms of meta-heuristics consist of intensification and diversification or (exploitation and exploration) [26]. Most meta-heuristic algorithms are nature-inspired and include Ant Colony Optimization (ACO), Particle Swarm Optimization (PSO) [27].

### **2.1 Meta-heuristic Method for Clustering**

Heuristic is a method that is faster than the classical method and can get a good approximation in many cases. By optimality, accuracy, completeness, or precision, an improvement may be achieved by more rapid trading. Heuristic thoughts and easy solutions are a shortcut for solving complex problems [28]. A meta-heuristic is a higher-level heuristic that is used to find, generate, or select a lower-level heuristic or procedure (partial search algorithm). and which might suggest a solution to an optimization problem, in particular with imperfect information and limited computational capacity [29].

Meta-heuristics often do not make any assumptions about the optimization problem being solved. As a result, they can be applied to a wide range of problems, compared to iterative methods and optimization algorithms, meta-heuristic is not capable of providing optimal solutions for all problem classes [30]. By implementing heuristic search methods in some ways, the found solution depends on the collection of random variables generated [31]. Meta-heuristic is able to search over a large set of feasible solutions with less computational efforts than iterative methods, algorithms, or simple heuristics. The k-means algorithm is improved by a meta-heuristic method [29].

## **3 Swarm Intelligence (SI)**

The best pattern discovery technology is based on optimization and important in information discovery and data mining (KDD). Cluster analysis is known as a quick and easy way to analyze complex data set. These datasets

are, in a way, very complex, and so there is an opportunity for clustering techniques to be applied. Different and various optimization techniques were used to examine clustering solutions. Swarm intelligence (SI) is one of the optimization approaches that has achieved tremendous success in different disciplines [32].

### 3.1 Computational Swarm Intelligence

Swarm Intelligence (SI) is an efficient computation paradigm suited for adaptive systems. This adds to genetic adaptation and social observation when discussing with the application of SI. In the literature, SI involves the installation of collective intelligence of groups of simple agents, which is applied to solve problem-solving tools such as the school's fish, bird flocks and insect colonies (like ants, termites and honeybees) by performing collective activities. In the 1980s, ethnologists conducted several studies in which they modeled the swarm behavior and concluded interesting observations. Each of the individuals within the swarm possesses a stochastic behavior in reaction to the perception of the environment. Local rules which are independent from the global rules and interactions between the self-organized agents lead to the emergence of collective intelligence. There is self-organization within swarms as the interactions on the local level lead to a global level response[33,34]. These trajectory tracking algorithms show how a decentralized, self-organized pattern can emerge in the collective foraging behavior of animals [35]. The major principles which express that swarm intelligence is an intelligent behavior are:

- The swarm is capable of both processing spatial and temporal data (the proximity principle).
- The swarm should be able to adapt to changing conditions, such as food quality and location (the principle of quality).
- The swarm should not provide all its resources to a narrow range of nodes, and should allocate the same resources to all the nodes in the swarm (the principle of diverse response).
- The swarm does not change its behavior if the environment is fluctuating (the stability principle).
- The swarm should have the capability to change itself whenever appropriate (the principle of adaptability) [36].

### 3.2 Particle Swarm Optimization (PSO)

PSO is both feasible and has successfully been implemented on other nonlinear problems like network training and fuzzy control [37]. When it comes to PSO, the elements form a collective swarm in finding a solution for the objectives. Every particle has two attributes, including the position and the velocity, which can be used to determine its future direction [38]. The population must continue the iteration process until the target is satisfied [39]. PSO also known as the bird's algorithm, as well as other meta-heuristic

algorithms, allow you to construct a random population of individuals and decide the optimal value for each individual. If a particle enters a new location from its previous location, it can be moved to the Personal Best, or the Global Best, or it can be moved directly to its previous location. [40].

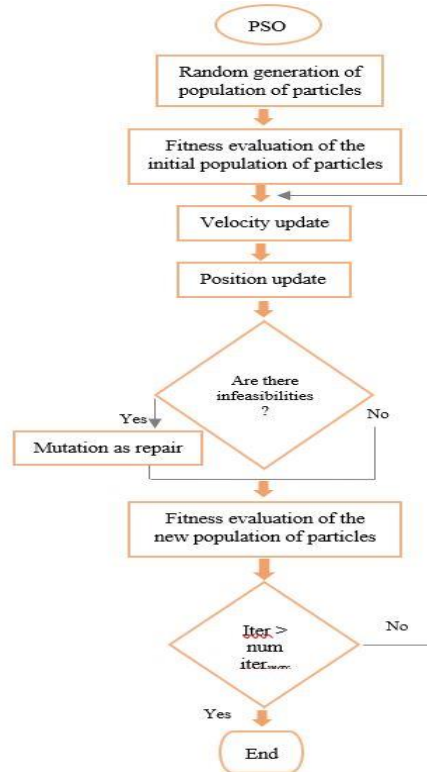


Figure 1: Flowchart PSO [41]

### 3.3 Artificial Bee Colony (ABC) Algorithm

The ABC algorithm was developed by Karaboga inspired by the activity of honeybee swarms. In the ABC colony, the bees can be arranged in three groups: workers, onlookers, and scouts. The half of the colony is mainly composed of workers, and the other half is made up of spectators. The actively employed bees are considered responsible for searching and analyzing food sources. They transfer their food to other insects such as bees. The onlookers pick the best food sources out of the foods that bees found in the first place. Once the quality of the natural food supply drops significantly, the bees will quit for a new source of food [42,43].

### 3.4 Ant Colony Optimization (ACO)

ACO is based on the natural behavior of ant-colony and individual workers. When ants are searching for food, it means they instinctively seem to determine the most optimum route to obtain food. This observed behavior is the basis for ACO. Imagine two ants walking for food down different ways to find food supply. When ants walk, they release airborne chemicals that cause decay over time. The ant which starts the trip in the direction of shorter route

will do so quicker than the other ant; thus, reinforcing the pheromone trail. These other ants will understand this signal and be influenced to follow the direction. According to [44], the ACO optimization algorithm has three major steps that constitute the core of the optimization phase.

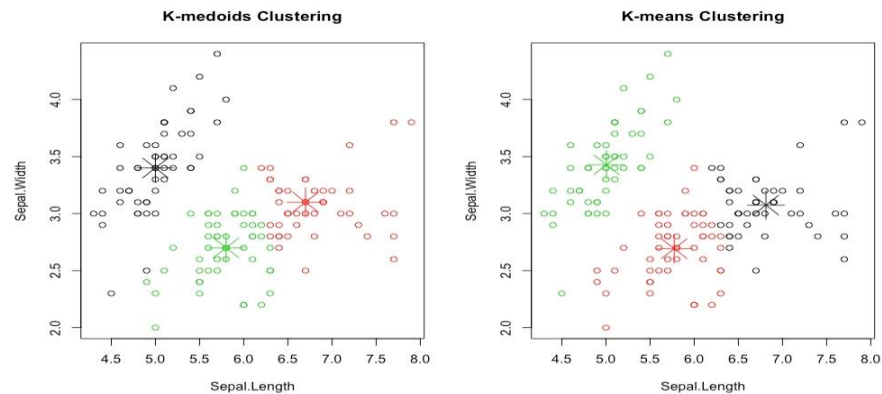
1. Constructor ants. This is the algorithm which "ants" use to accomplish some sort of development or improvement by way of self-organization or growth.
2. Pheromone evaporates. This is the process in which pheromones are reduced by using "local" information for certain solutions; this step is also often called a local update. This step ensures that the ACO does not converge prematurely to a single solution.
3. Daemon Actions. This one is known as decisions involving global information on the problem of optimization. Note the difference between local and global in this example. Like step 2, step 3 is also referred to as global update.

#### **4 Clustering Algorithms**

Data clustering is a study area that is widely approached in data mining and ML fields because it is applied to segmentation, summarization, learning, information retrieval, pattern recognition and target marketing, data mining [25,46,47,48], and text mining [49,50]. The clustering algorithms are divided into two categories, including hierarchical clustering and partitional clustering [51]. Clustering algorithms group sets of objects so that objects in a given set or cluster share more similarity than the objects of other clusters. Clustering is primarily executed in exploratory data mining and this strategy is utilized usually for analyzing statistical data, and it is exploited in a number of domains like ML, retrieving the information, pattern recognizing, bioinformation, and analyzing image [14,52]. Cluster analysis is a general task to be fulfilled. This task may be accomplished by a variety of algorithms which differ significantly in terms of the notion which is relevant to constituting a cluster and the method of discovering them. The cluster model typically involves short distances between the cluster components, condensed areas within data space and certain statistical distributions [53,54].

Clustering analysis is the most predominant tool in microarray data analysis, that can group genes with similar expression patterns but under different experimental settings or taken from other tissues because genes with analogous expression profiles commonly function similarly, genes that have unknown functions are predictable based on the resulting class [55]. Clustering is exploited in many fields, for instance retrieving information [56,57]. Clustering are helpful in finding more rapidly relevant information [58]. It helps scholars to be updated with the newest discoveries in their research areas. In the recent period, clustering has drawn the attention of numerous scholars due to its applications in classifying, decision making, extracting information, and analyzing patterns [59]. However, the shared

starting point is that they are groups of data objects. As found by different algorithms, cluster concept considerably shows a discrepancy in its features. Understanding such "cluster models" leads to understanding variations found among various algorithms [60,61]. For each cluster, the single-sample approaches provide an example and assign data points that minimize the number of distances between data points and their closest examples. A common method for k-means is k-medoids clustering, which is very similar to k-means [62]. Figure 1 Differentiates between the k-mean and k-medoid of a cluster.



**Figure 2:** Differentiates between the k-mean and k-medoid of a cluster [62]

### K-means Vs K-medoids

- Both require K to be specified in the input.
- K-medoids eliminates outliers in the data.
- K-medoids is more expensive to perform.
- Both methods assign each instance exactly to one cluster.

Fuzzy partitioning techniques relax this

- Partitioning methods generally are good at finding spherical shaped clusters.
- They are suitable for small and medium sized datasets.

Extensions are required for working on large data sets [62].

### 4.1 K-Means

K-means clustering, commonly used for data mining analysis, is a method of vector quantizing originating from signal treatment. The objective of K-means is to divide  $n$  observations into  $K$  clusters; all observations are part of the cluster that works as a prototype of a Cluster[63]. The K-Means Approach is commonly used and is an iterative process that begins with the initial partitioning and then converges on the best results with decreasing the sum squared error (SSE) [64,65]. The problem has proved to be an NP-hard problem. While there are several effective heuristic algorithms that are able to quickly find the algorithm is equivalent to the expectation-maximization algorithm because of the methods evaluated of how they move towards a global optimum through an iterative refinement method [66].

The objective of the classical K-means clustering method is find the set  $C$  of  $K$  clusters  $C_j$  with cluster mean  $c_j$  for the sake of decreasing the amount of the squared errors [17]. As show in Equation 1.

$$E = \sum_i^k = 1 \sum_{xi \in C_j} \|c_j - xi\|^2 \tag{1}$$

$E$  is the addition of (SSE) of objects having cluster means for  $K$  cluster,  $\| \dots \|$  refers to distance Mertie between a cluster mean and a data point  $xi$   $C_j$ . As show in Equation 2.

$$\|x - y\| = \sqrt{\sum_{i=1}^p |xi - yi|^2} \tag{2}$$

A flowchart of K-means clustering has been illustrated which is made up of six essential stages. First, preliminary value of centroids: Let ( $C_1, C_2, \dots$ ) represents centroids harmonize. Second, the objects' distance is calculated using the cluster centroid and the objects in the cluster. The distance Euclidean is used and the distance matrix is then calculated with the iteration 0. Each column in the matrix of distance means an object. The distance of matrix in the first row matches the distance of every object to the 2nd row and the first centroid stands for the distance of every object in the 2nd centroid. At 3rdrow, clustering of objects: Allocate every object on the basis of least distance. At 4throw iteration-1, determining the centroids: by identifying the components of all groups, the new centroid of every set and it is computed on the basis of these memberships which are new. At fifth row, repeating from step 2. At sixth row, the last iteration grouping is compared and this iteration states that groups are not moved by the objects So, K- means clustering computation means that it has become stable and there is no need of iteration anymore [17].

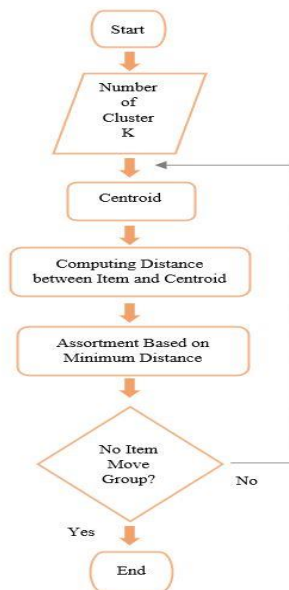


Figure 3: Flowchart of K-means Clustering [17]



## 4.2 Related Work of K-Means

Despite the fact that MacQueen used the term "K-means" for the first time in 1967 [66] the idea dates back to Steinhaus in 1957 [67]. The pulse-coding modulation standard algorithm has been proposed for the first time by Lloyd in 1957; though, it was not published until 1982 [68]. Moreover, Forgy published the same approach for its similarity in 1965, and this why it is sometimes named after him [69]. While Hartigan (1979) also published a more efficient version. Standard K-means algorithms employ the strategy of iterative refinement. Due to its pervasiveness, it is called K-means algorithm and also Lloyd's algorithm, particularly in computer sciences. At the beginning, the algorithm is offered a set of K-means  $m_1, m_k$ , then it continues by alternating between two stages [70]. The first stage is allocating where every observation is allocated to a cluster that its mean gives up the minimum within-cluster sum of squares (WCSS). As sum of squares is the squared Euclidean distance, it is called "nearest" mean [71].

The second stage is the updating where new means are estimated to stand for the centroids of the observations within the new clusters. When the allocating no longer changes, the algorithm can be called converged. Since both stages optimizes WCSS objective and there is only a finite number of partitioning, the algorithm is supposed to be altered to a (local) optimum. By using this algorithm, the global optimum cannot be guaranteed to be found [72]. Initialization approaches utilized in K-means algorithm are Forgy and Random Partition [69]. Believe that typically the random partition approach is favorable for instance, regarding K-harmonic means and fuzzy K-means. Forgy's approach of initialization for standard K-means and expectation maximization algorithms is superior to existing approaches.[73].

Since it is an exploratory algorithm, its convergence to the global optimum is not assured; and the outcomes may rely on the preliminary clusters [74]. Since this algorithm is typically so quick, it is usually executed more than one time with different beginning conditions. However, in its very bad cases, K-means so slowly converges [75]. One concern with the K-means clustering algorithm is that it could result in large intra-cluster distances. Therefore, the distance between members of cluster and the cluster center is long and members of cluster are different from each other. To solve this problem the optimization algorithm can be used. A few of the optimization methods is PSO, that provides better results. In addition, to this problem. A hybrid of PSO and K-means clustering algorithm can be used to solve the problem, and any problems can be eliminated [76].

Table 1 shows which methods have been proposed in the literature to increase the accuracy of k-means clustering algorithm.

**Table 1: Meta-Heuristic Review for K-means Clustering**

Ref.	Year	Methods	Problems	Datasets	Results
[77]	2020	<ul style="list-style-type: none"> <li>○ PSO</li> <li>○ PSOFKM</li> <li>○ PSOLF-KHM</li> <li>○ PSOM</li> </ul>	Initiating the cluster centres, catch up with local point of optimum.	<ul style="list-style-type: none"> <li>○ IRIS</li> <li>○ WINE</li> <li>○ GLASS</li> <li>○ HEART</li> <li>○ CANCER</li> <li>○ ECOLI</li> <li>○ CREDIT</li> <li>○ YEAST</li> </ul>	PSOM is able to solve the best compared to PSO, PSOFKM and PSOLF-KHM for all datasets.
[78]	2020	<ul style="list-style-type: none"> <li>○ A novel (Uk-means)</li> </ul>	A variety of K-means and its extensions are always affected by initializations and a necessary number of clusters a priori.	<ul style="list-style-type: none"> <li>○ Synthetic Datasets</li> <li>○ UCI Datasets</li> <li>○ Medical Datasets</li> <li>○ Image Datasets</li> </ul>	The actual results indicate that the U-k-means clustering algorithm is more efficient.
[79]	2020	<ul style="list-style-type: none"> <li>○ ABC</li> <li>○ ACO</li> <li>○ BBO</li> <li>○ CA</li> <li>○ DE</li> <li>○ GA</li> <li>○ HS</li> <li>○ IWO</li> <li>○ PSO</li> <li>○ TLBO</li> </ul>	Making the most suitable cluster centroids is a key goal for a successful k-means clustering operation.	<ul style="list-style-type: none"> <li>○ synthetic dataset</li> <li>○ real-world datasets</li> </ul>	A comparison is performed on various real-world datasets.
[80]	2020	<ul style="list-style-type: none"> <li>○ PSO</li> <li>○ K-means</li> </ul>	Image is de-noised and colorized.	<ul style="list-style-type: none"> <li>○ Lena</li> <li>○ Tree</li> <li>○ Flower</li> </ul>	The algorithm can segment images with higher accuracy and higher efficiency than (PSOK).
[81]	2019	<ul style="list-style-type: none"> <li>○ SK-means</li> <li>○ EM</li> <li>○ PSO</li> <li>○ SCPSO</li> </ul>	The problem of internal inconsistency in group of documents in a variety of areas.	<ul style="list-style-type: none"> <li>○ Reuters</li> <li>○ 20Newsgroup</li> <li>○ TDT2</li> </ul>	The proposed SCPSO algorithm is better than other techniques for clustering.
[82]	2019	Combined PSO with K-means (PSOKM)	Clustering analysis groups, the text into similar clusters, and the text in different clusters are the most dissimilar.	<ul style="list-style-type: none"> <li>○ SSE</li> <li>○ XB</li> <li>○ DB</li> </ul>	PSOKM does better than the others.
[83]	2019	<ul style="list-style-type: none"> <li>○ CLARA</li> <li>○ K-Means</li> </ul>	Comparing two techniques, (CLARA) clustering and K-Means clustering.	<ul style="list-style-type: none"> <li>○ Iris</li> </ul>	CLARA clustering is better than the K-Means.

[84]	201	<ul style="list-style-type: none"> <li>○ AC Clustering</li> <li>○ GA Clustering</li> <li>○ Firefly Algorithm</li> <li>○ Firefly Clustering</li> </ul>	NP hard problem: find minimum tour length and return to starting node.	<ul style="list-style-type: none"> <li>○ eil51</li> <li>○ eil76</li> <li>○ pr76</li> <li>○ ulysse16</li> </ul>	Prove the effectiveness of k-means clustering in solving the TSP with the k-means algorithm.
[85]	2018	<ul style="list-style-type: none"> <li>○ GA</li> <li>○ PSO</li> <li>○ GODLIKE</li> </ul>	Main characteristic or similarity regions of an image segmentation.	<ul style="list-style-type: none"> <li>○ Mountain</li> <li>○ Pepper</li> <li>○ Lena</li> <li>○ Boat</li> <li>○ Cameraman</li> <li>○ Brain</li> <li>○ Outdoor</li> <li>○ Building A</li> <li>○ Building B</li> </ul>	The simulation result showed that the proposed method provides better output.
[86]	2017	<ul style="list-style-type: none"> <li>○ PS-BCO-K</li> <li>○ K-PS-BCO</li> </ul>	Data clustering	<ul style="list-style-type: none"> <li>○ Iris</li> <li>○ Wine</li> <li>○ Cancer</li> <li>○ CMC</li> <li>○ HV</li> </ul>	The proposed algorithms give a more accurate quality solution than some well-known heuristic algorithms.

## 5 Discussion

From the literature that has been done above it is shown that the metaheuristic algorithms are proved efficient at finding the local optima problem of the group clustering. However, because these algorithms are implemented empirically and their effectiveness is proved by the research, it is not up to challenge their efficiency. A review and study on the K-means algorithm found some shortcomings. The main objective of the above table is to review the K-means algorithm and meta-heuristic algorithms to improve the K-means algorithm. The main focus is on the clustering algorithm review. The metrics in the studies are reviewed. The databases that were used are investigated. One of the ways to reduce the shortcomings of the K-means clustering is by using hybrid method.

Based on the review that has been done earlier, several authors suggested methods to address the shortcomings of partitional clustering issue without unique data and sample such that optimum number of clusters can be computed. Metaheuristic approaches proved that it could get rid of such problems as aforementioned. This is since metaheuristic algorithms can detect and use the local optima and can provide an efficient solution for finding number of clusters in the specified dataset. Based on the table it has been shown that the PSO method has been used in many studies to overcome the shortcomings of clustering methods. The study of [79] has used several optimization techniques to improve the k-means clustering, based on the

evaluation results it has been shown that the PSO method has got higher results compared to other techniques such as ABC, ACO, GA, and so on. The study of [80] used k-means method in segmentation task, then combined PSO with k-means called (PSOK) which got higher results. More so, based on the study [84], it has been proven that the firefly technique also can improve the k-means, where they used ACO, GA, Firefly, and each of them with k-means in TSP solution, it is shown that firefly can improve K-means better than other techniques.

## 6 Conclusion

A literature study on the efficacy of K-means showed that this technique has some shortcomings. As K-means is a popular clustering algorithm due to its simplicity and efficiency, there is a need for its improvement. The K-means clustering algorithm can be applied with meta-heuristic algorithms to enhance the performance, Since the clustering algorithm is an unsupervised algorithm, it is more efficient in gathering information than algorithms used for improved K-means which have extra information necessary to solve problem.

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